CS 2731 Introduction to Natural Language Processing

Session 10: N-gram language models, part 1

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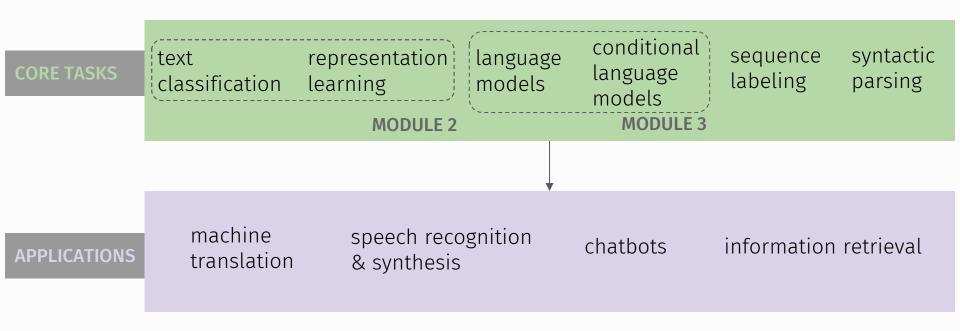
Course logistics

- Homework 2 is due next Thu Oct 3
 - Text classification
 - Written and programming components
 - Optional Kaggle competition for best LR and NN deception classifiers
- Project ranking form is due tomorrow, Thu Sep 26

Lecture overview: N-gram language models, part 1

- Language modeling
- N-gram language models
- Estimating n-gram probabilities
- Perplexity and evaluating language models

Core tasks and applications of NLP



Introduction to language models

Language Models Estimate the Probability of Sequences

Which of these sentences would you be more likely to observe in an English corpus?

- · Hugged I big brother my.
- I hugged my large brother.
- I hugged my big brother.



Language Models Estimate the Probability of Sequences

Which of following word would be most likely to come after "David hates visiting New..."

- York
- · California
- giggled





These are actually instances of the same problem: the language modeling problem!

Language Modeling is Tremendously Useful

LMs (language models) are at the center of NLP today and have many different applications

- Machine Translation
 P(high winds tonight) > P(large winds tonight)
- Spelling Correction
 P(about fifteen minutes from) > P(about fifteen minutes from)
- Text Input Methods
 P(i cant believe how hot you are) > P(i cant believe how hot you art)
- Speech Recognition
 P(recognize speech) > P(wreck a nice beach)

The Goal of Language Modeling

Compute the probability of a sequence of words/tokens/characters:

$$P(\mathbf{w}) = P(w_1, w_2, w_3, w_5, \dots, w_n)$$

P(I, hugged, my, big, brother)

This is related to next-word prediction:

$$P(W_t|W_1W_2...W_{t-1})$$

P(York|David, hates, going, to, New)

Do you compute either of these? Then you're in luck:

N-gram language models

The Chain Rule Helps Us Compute Joint Probabilities

The definition of conditional probability is

$$P(B|A) = \frac{P(A,B)}{P(A)}$$

which can be rewritten as

$$P(A, B) = P(A)P(B|A)$$

The Chain Rule Helps Us Compute Joint Probabilities

If we add more variables, we see the following pattern:

$$P(A, B, C) = P(A)P(B|A)P(C|A, B)$$

$$P(A, B, C, D) = P(A)P(B|A)P(C|A, B)P(D|A, B, C)$$

which can be generalized as

$$P(x_1, x_2, x_3, \dots, x_n) = P(x_1)P(x_2|x_1)P(x_3|x_1, x_2)\dots P(x_n|x_1, \dots, x_{n-1})$$

The chain rule to compute the joint probability of words in a sentence

$$P(w_1, w_2, w_3, \dots, w_n) = \prod_{i=1}^{n} P(w_i | w_1 w_2 \dots w_{i-1})$$

P(now is the winter of our discontent) =

 $P(\text{now}) \times P(\text{is}|\text{now}) \times$

 $P(\text{the}|\text{now is}) \times P(\text{winter}|\text{now is the}) \times$

 $P(\text{of}|\text{now is the winter}) \times$

 $P(\text{our}|\text{now is the winter of}) \times$

P(discontent|now is the winter of our)



How Are We Estimating these Probabilities?

Could we just count and divide?

P(discontent|now is the winter of our) = Count(now is the winter of our discontent) Count(now is the winter of our)

But this can't be a valid estimate! "now is the winter of our" is going to very rare in corpora. It isn't going to be a good estimate of its true probability.

This May not Seem Very Helpful

Is P(discontent|now is the winter of our) really easier to compute than P(now is the winter of our discontent)?

How can the chain rule help us? We can cheat.

Enter a Hero: Andrei Markov



20 December 1978 Born (age 43) Voskresensk, Russian SFSR, Soviet Union

Height 6 ft 0 in (183 cm)

Weight 203 lb (92 kg; 14 st 7 lb)

Position Defence

Played for Khimik

Voskresensk Dynamo Moscow

Montreal Canadiens

Vityaz Chekhov

Ak Bars Kazan

Lokomotiv Yaroslavl

Playing career

1995-2020

Or, Rather, Andrey Markov



Born 14 June 1856 N.S.

Ryazan, Russian

Empire

Died 20 July 1922 (aged

66) Petrograd,

Russian SFSR

Known for Markov chains;

Markov processes;

stochastic

processes

Fields Mathematics,

specifically

probability theory

and statistics

Doctoral advisor Pafnuty

Chebyshev

Slide credit: David Mortensen

Markov Did a Computational Linguistics

Interestingly, Markov's first application of his idea of **Markov Chains** was to language, specifically to modeling alliteration and rhyme in Russian poetry.

As such, he can be seen not only as a great mathematician and statistician, but also one of the forerunners of computational linguistics and computational humanities.



Markov Showed that You Could Make a Simplifying Assumption

One can approximate

P(discontent|now is the winter of our)

by computing

P(discontent|our)

or perhaps

P(discontent|of our)

- We only get an estimate this way, but we can obtain it by only counting simpler things: "our discontent", "discontent", "of our", etc.
- Ngram language modeling is a generalization of this observation

This assumption is the Markov assumption

$$P(W_1, W_2, ..., W_n) \approx \prod_{i} P(W_i | W_{i-k} W_{i-1})$$

In other words, we approximate each component in the product:

$$P(W_i|W_1, W_2, \dots, W_{i-1}) \approx P(W_i|W_{i-k} \dots W_{i-1})$$

We will now walk through what this looks like for different values of k.

The Unigram Model (k = 1)

$$P(W_1W_2...W_i) \approx \prod_i P(W_i)$$

The probability of a sequence is approximately the product of the probabilities of the individual words.

Some automatically generated sequences from a unigram model:

- fifth, an, of, futures, the, an, incorporated, a, a, the, inflation, most, dollars, quarter, in, is, mass
- thrift, did, eighty, said, hard, 'm, july, bullish
- that, or, limited, the

The Bigram Model (k=2)

If you condition on the previous word, you get the following:

$$P(W_i|W_1W_2...W_{i-1}) \approx P(W_i|W_{i-1})$$

Some examples generated by a bigram model:

- texaco, rose, one, in, this, issue, is, pursuing, growth, in, a, boiler, house, said, mr., gurria, mexico, 's, motion, control, proposal, without, permission, from, five, hundred, fifty, five, yen
- · outside, new, car, parking, lot, of, the, agreement, reached
- · this, would, be, a, record, november

The Trigram Model

The trigram model is just like the bigram model, only with a larger k:

$$P(w_i|w_1w_2...w_{i-1}) \approx P(w_i|w_{i-2}w_{i-1})$$

The output of a trigram language model is generally **much** better than that of a bigram model **provided the training corpus is large enough**. Why do you need a larger corpus to train a trigram corpus than a bigram or unigram corpus?

N-gram models have trouble with long-range dependencies

In general, n-gram models are very impoverished models of language. For example, language has relationships that span many words:

- The students who worked on the assignment for three hours straight *is/are finally resting.
- The teacher who might have suddenly and abruptly met students is/*are tall.
- · Violins are easy to mistakenly think you can learn to play *them/quickly.

Ngram LMs Are Often Adequate

Nevertheless, for many applications, ngram models are good enough (and they're super fast and efficient)

Estimating n-gram probabilities

Estimating bigram probabilities with the maximum likelihood estimate (MLE)

MLE for bigram probabilities can be computed as:

$$P(w_i|w_{i-1}) = \frac{\operatorname{count}(w_{i-1}, w_i)}{\operatorname{count}(w_{i-1})}$$

which we will sometimes represent as

$$P(W_i|W_{i-1}) = \frac{C(W_{i-1}, W_i)}{C(W_{i-1})}$$

An example

$$\begin{array}{ll} P(\texttt{I}\,|\,\texttt{~~}) = & P(\texttt{Sam}\,|\,\texttt{~~}) = & P(\texttt{am}\,|\,\texttt{I}) = \\ P(\texttt{~~}\,|\,\texttt{Sam}) = & P(\texttt{Sam}\,|\,\texttt{am}) = & P(\texttt{do}\,|\,\texttt{I}) = \end{array}~~$$

More examples: Berkeley Restaurant Project sentences

can you tell me about any good cantonese restaurants close by mid priced thai food is what i'm looking for tell me about chez panisse can you give me a listing of the kinds of food that are available i'm looking for a good place to eat breakfast when is caffe venezia open during the day

Raw bigram counts

Out of 9222 sentences

	i	want	to	eat	chinese	food	lunch	spend
i	5	827	0	9	0	0	0	2
want	2	0	608	1	6	6	5	1
to	2	0	4	686	2	0	6	211
eat	0	0	2	0	16	2	42	0
chinese	1	0	0	0	0	82	1	0
food	15	0	15	0	1	4	0	0
lunch	2	0	0	0	0	1	0	0
spend	1	0	1	0	0	0	0	0

Slide adapted from Jurafsky & Martin

Raw bigram probabilities

Normalize by unigrams:

Result:

i	want	to	eat	chinese	food	lunch	spend
2533	927	2417	746	158	1093	341	278

	i	want	to	eat	chinese	food	lunch	spend
i	0.002	0.33	0	0.0036	0	0	0	0.00079
want	0.0022	0	0.66	0.0011	0.0065	0.0065	0.0054	0.0011
to	0.00083	0	0.0017	0.28	0.00083	0	0.0025	0.087
eat	0	0	0.0027	0	0.021	0.0027	0.056	0
chinese	0.0063	0	0	0	0	0.52	0.0063	0
food	0.014	0	0.014	0	0.00092	0.0037	0	0
lunch	0.0059	0	0	0	0	0.0029	0	0
spend	0.0036	0	0.0036	0	0	0	0	0

Bigram estimates of sentence probabilities

```
P(<s> I want english food </s>) =
P(||<s>)
      × P(want|I)
      × P(english|want)
      × P(food|english)
      \times P(</s>|food)
    = .000031
```

Multiplication Considered Harmful

In reality, as was the case with NB classification, we do all of our computation in log space

- Avoid underflow Multiplying small probabilities by small probabilities results in very small numbers, which is problematic
- Optimize computation Addition is cheaper than multiplication

$$\log(p_1 \times p_2 \times p_3 \times p_4) = \log p_1 + \log p_2 + \log p_3 + \log p_4$$

The are high-performance toolkits for n-gram language modeling

- SRILM http://www.speech.sri.com/projects/srilm/
- KenLM https://kheafield.com/code/kenlm/

Perplexity and evaluating language models

The Evaluation Process for ML Models

The goal of LM evaluation:

- Does our model prefer good sentences to bad sentences?
- Specifically, does it assign higher probabilities to the good/grammatical/frequently observed ones and lower probabilities to the bad/ungrammatical/seldom observed ones?

In ML evaluation, we divide our data into three sets: train, dev, and test.

- We train the model's parameters on the **train** set
- · We tune the model's hyperparameters (if appropriate) on the dev set (which should not overlap with the train set
- · We test the model on the **test** set, which should not overlap with train or dev

We Can Evaluate Models Intrinsically or Extrinsically

- Extrinsic Evaluation means asking how much the model contributes to a larger task or goal. We may evaluate an LM based on how much it improves machine translation over a BASELINE.
- Intrinsic Evaluation means measuring some property of the model directly. We may quantify the probability that an LM assigns to a corpus of text.

In general, EXTRINSIC EVALUATION is better, but more expensive and time-consuming.

Extrinsic Evaluation of LMs

Best evaluation for comparing models A and B

- Put each model in a task (spelling corrector, speech recognizer, MT system)
- Run the task, get an accuracy for A and for B
 - How many misspelled words corrected properly?
 - · How many sentences translated correctly?
- Compare scores for A and B

This takes a lot of time to set up and can be expensive to carry out.

Perplexity is an intrinsic metric for language modeling

Perplexity evaluates the probability assigned by a model to a collection of test documents, controlling for length and is, thus, useful for evaluating LMs.

A better model of a text is one which assigns a higher probability to words that actually occur in the test set. This will result in **lower** perplexity.

However:

- · It is a rather crude instrument
- It sometimes correlates only weakly with performance on downstream tasks
- It's only useful for pilot experiments
- · But it's cheap and easy to compute, so it's important to understand

Deriving Perplexity for Bigrams

$$PP(\mathbf{w}) = P(w_1 w_2 \dots w_n)^{-\frac{1}{n}}$$
 Definition
$$= \sqrt[n]{\frac{1}{P(w_1 w_2 \dots w_n)}}$$

$$= \sqrt[n]{\prod_{i=1}^{n} \frac{1}{P(w_i | w_1 w_2 \dots w_{i-1})}}$$
 Chain Rule
$$= \sqrt[n]{\prod_{i=1}^{n} \frac{1}{P(w_i)}}$$
 For Unigrams
$$= \sqrt[n]{\prod_{i=1}^{n} \frac{1}{P(w_i | w_{i-1})}}$$
 For Bigrams

To minimize perplexity is to maximize probability!

Perplexity as branching factor

- Let's suppose a sentence consisting of random digits
- What is the perplexity of this sentence according to a model that assign P=1/10 to each digit?

$$PP(W) = P(w_1 w_2 ... w_N)^{-\frac{1}{N}}$$

$$= (\frac{1}{10}^N)^{-\frac{1}{N}}$$

$$= \frac{1}{10}^{-1}$$

$$= 10$$

In general, a lower perplexity implies a better model.

Intuition of Perplexity

Perplexity evaluates how well our language model can predict the next words in our test set

I always order pizza with cheese and ____

The Shannon Game



mushrooms 0.1 pepperoni 0.1 anchovies 0.01

fried rice 0.0001

and 1e-100

Lower perplexity = better model

Training 38 million words, test 1.5 million words, WSJ

N-gram Order	Unigram	Bigram	Trigram
Perplexity	962	170	109

Questions?